

Transit-timing variations of exoplanet Kepler-410 Ab

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Introduction

- exoplanets – one of the main topics of current astrophysical research
- multiple projects focused on the search of exoplanets (*Kepler*, *TESS*, etc.)
- 3925 confirmed exoplanets, 657 planetary systems
- wide scope for further research
- study dynamics and stability of the planetary systems → their formation and evolution
- resonant interaction – a key factor of the orbital stability

Methods for searching for exoplanets

- transits
 - the simplest and most successful method (mission *Kepler*)
 - watching for the regular drops of the brightness of the parent star
- radial velocities (RV)
 - the shift of the spectral lines as the result of the Doppler effect
 - determination of the mass of the planet (combination with transits)
- transit-timing variations (TTV)
 - gravitational interactions of the another body in the system

Mean-motion resonances

- small but regular perturbation has a significant influence on the behaviour of the studied body
- mean-motion resonance (MMR) – if the ratio (at least approximately) works

$$\frac{P_1}{P_2} = \frac{n_2}{n_1} = \frac{p}{p - q}$$

- the most common type of resonance – planets, moons, asteroids, etc.
- bodies are regularly in the same configuration
- significantly affects the stability of the system – stabilize or destabilize orbit

Effect of resonances on the TTV

- resonances – the main source of the TTV in the known exoplanetary systems
- period of the TTV depends on the distance from the exact MMR

$$P_{\text{TTV}} = \frac{1}{|p/P_1 - (p-q)/P_2|}$$

- amplitude of the TTV of the 1st planet caused by the 2nd planet depends mainly on the mass of the 2nd planet and the order of the resonance

$$\delta t_1 \propto P_1 \frac{m_2}{M_\star} \frac{a_1}{a_2} f(a_1, a_2, P_1, P_2)$$

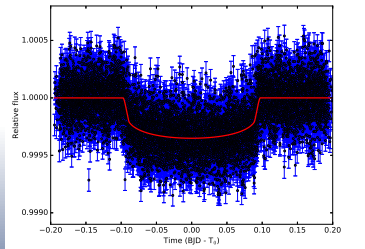
- determination of the masses of two transiting exoplanets in the resonance (both with TTV)
- if only one planet \Rightarrow unknown order of the resonance \Rightarrow we cannot exactly tell what planet causes TTV

Numerical simulations

- solving the n -body problem – no analytical solution
- numerical integration of the orbits – e.g. using package Mercury6 or Swift
- wide opportunities in celestial mechanics
- commonly used also in the study of exoplanetary systems:
 - simulation of TTV
 - resonant interaction between planets
 - long-term stability of the planetary systems

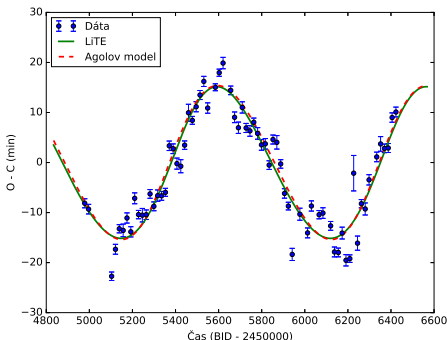
Exoplanetary system Kepler-410

- brightness V 9.5 mag
- distance 148.16 ± 0.49 pc (GAIA - DR2)
- Kepler-410 A – $1.352 R_{\odot}$, $1.214 M_{\odot}$, spectral type F6IV
- Kepler-410 B (Adams *et al.*, 2012) – distance $1.63'' \Rightarrow 250$ AU;
a red dwarf (4850 K)
- transiting exoplanet Kepler-410 Ab
 - discovered in 2013 (Van Eylen *et al.*, 2014)
 - size of Neptune – $2.647 R_{\oplus}$
 - orbital period – 17.8336313 d
 - semi-major axis – 0.1426 AU



TTV

- amplitude ≈ 15 min., period 970 – 975 days
 - studied also in a paper Gajdoš *et al.* (2017) using two analytical models:
- 1 Light-Time effect (Irwin, 1952) – $M_3 \approx 2.1 M_\odot$
 - 2 model by Agol *et al.* (2005) – $M_3 \approx 0.9 M_\odot$
- ⇒ another body with stellar mass on the orbit with orbital period 970 days

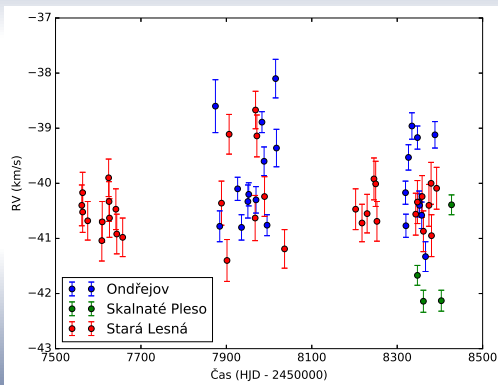


RV measurements

- expected variation with an amplitude $25 - 30$ km/s and a period ~ 970 days
- measurements from three observatories (SR+ČR) during three observing seasons (2016 – 2018)

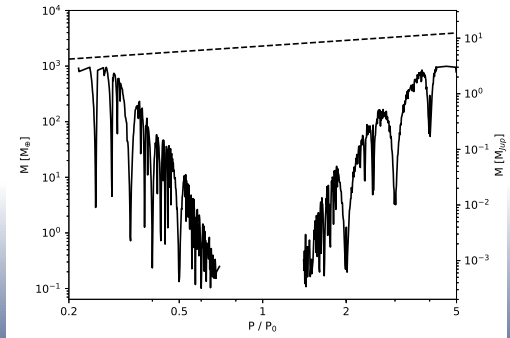
RV measurements

- expected variation with an amplitude 25 – 30 km/s and a period ~ 970 days
- measurements from three observatories (SR+ČR) during three observing seasons (2016 – 2018)
- from the observations – amplitude $\lesssim 600 - 800$ m/s
- the stellar originator of TTV could be excluded
- the existence of close brown dwarf or massive hot jupiter is also unlikely



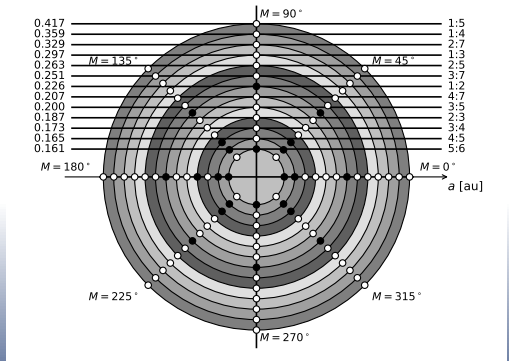
Resonant interaction

- another interpretation of observed TTV \rightarrow resonances between exoplanet Kepler-410 Ab and other (unknown) planet
- analysis using numerical simulations
- determination of the mass of the planet for different orbital periods
- in MMR – small planets with a mass $0.1 - 3 M_{\oplus}$
- many possible explanations – different couples of M , P
- RV measurements – no constraint on a range of possible planets



Stability of the resonance

- determine the most probable explanation of TTV caused by the resonances
- studying long-term stability (5000 years) of the significant MMR
- interior resonances are less stable
- most of exterior resonances are stable
- resonance 1:2 is unstable



Conclusions

- observed variations of the times of transit of exoplanet Kepler-410 Ab
- RV measurements excluded existence of another close star \Rightarrow rejection of the previous explanation of TTV (Gajdoš *et al.*, 2017)
- possible origin of TTV – small planet close to the MMR
- determine the most probable option – stability of the resonances + statistical distribution of resonances among the known systems (Wang & Ji, 2014)
- explanation of TTV - a planet with a mass of $1.5 M_{\text{Mars}}$ close to the exterior resonance 2:3 (period 26.5 days)
- hardly detected by current instruments
- results already published in a paper Gajdoš *et al.* (2019)

Thank you for your attention!

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